

# Intranuclear cascade model for cluster production reaction

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# Intranuclear cascade (INC) model

Spallation reactions at intermediate-energies

DDX of  $(p,p'x)$ ,  $(p,nx)$ , , ,

nucleon spectra from nucleon-induced reactions

reasonable prediction in a wide energy range

Particle transport simulation; PHITS, Geant4, ...

Intensive developments of simulation tools require predictive power in cluster productions.

INC advantage = high flexibility  $\neq$  exact theory

Extension toward any direction

physics modeling:

reasonable, appropriate, consistent, , ,

→ generalization; target, energy, cluster

Deep understanding of the process is essential.

Physics model in INC :

succession of binary hard collisions

Repulsive interaction

No attractive interaction

Cluster formation is not included.

Do we add an attractive interaction?

1<sup>st</sup> question

INC = binary hard collisions

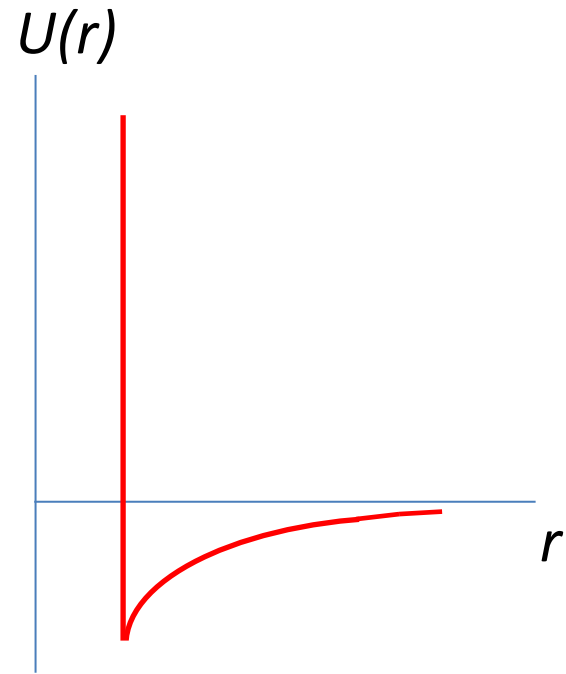
What is the hard collision?

hard repulsive core

Large  $q$

→ continuum state

- particle like picture

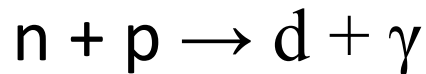


Soft collision = shallow part of potential  
potential scattering ; elastic, inelastic  
direct reaction wave function

- wave like picture

Clustering;

Which picture, particle or wave ?



No chance for classical particles to be bound at positive energies.

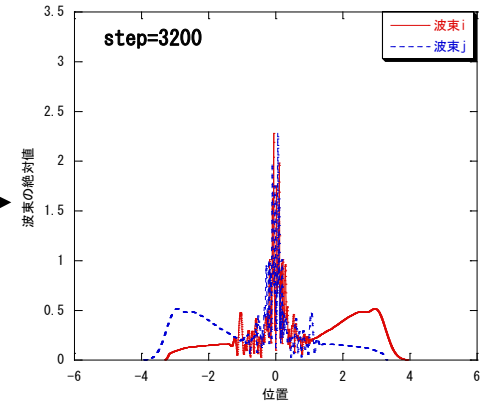
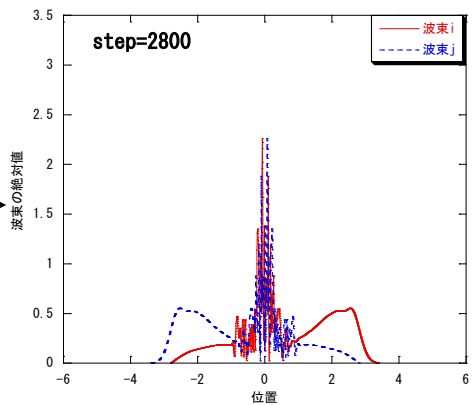
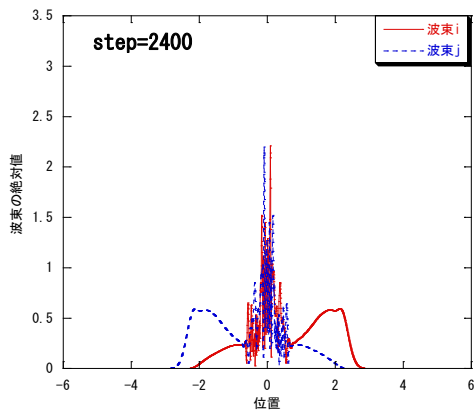
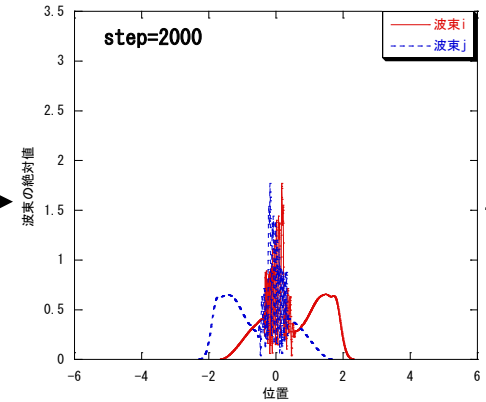
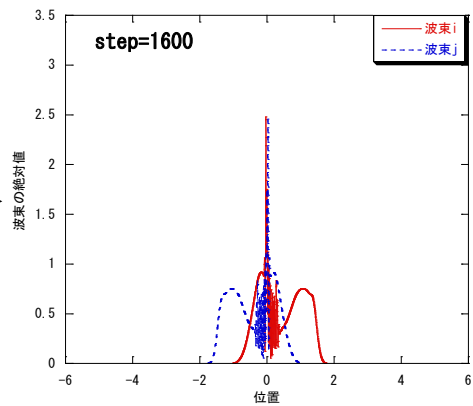
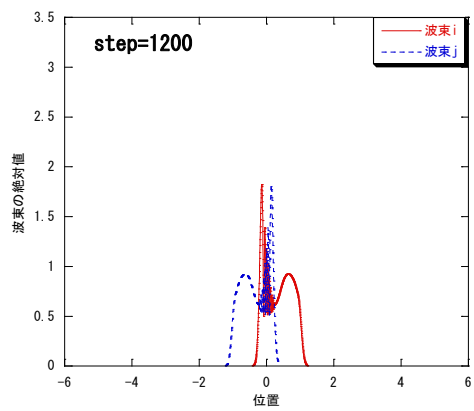
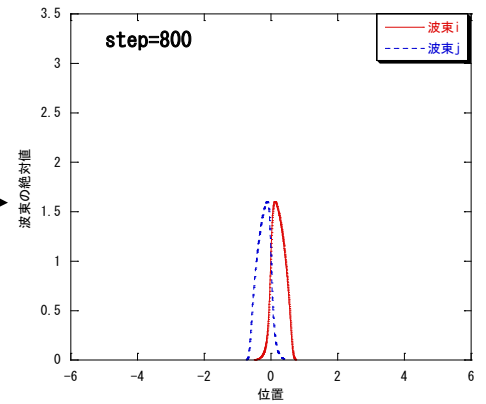
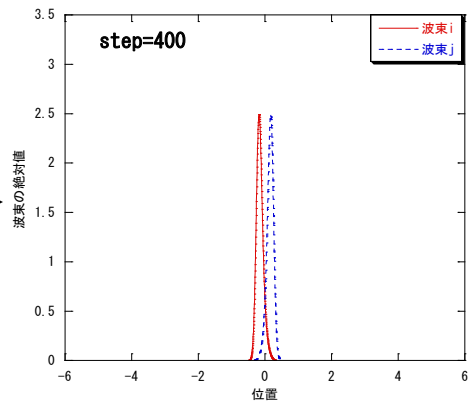
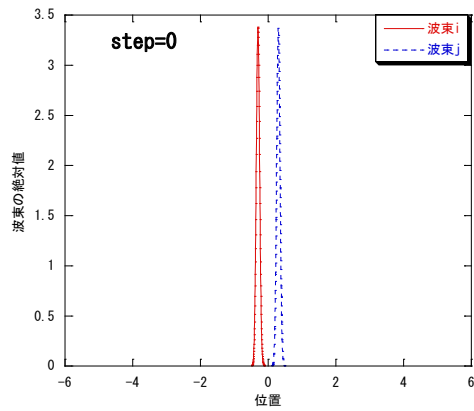
 attractive force is not essential

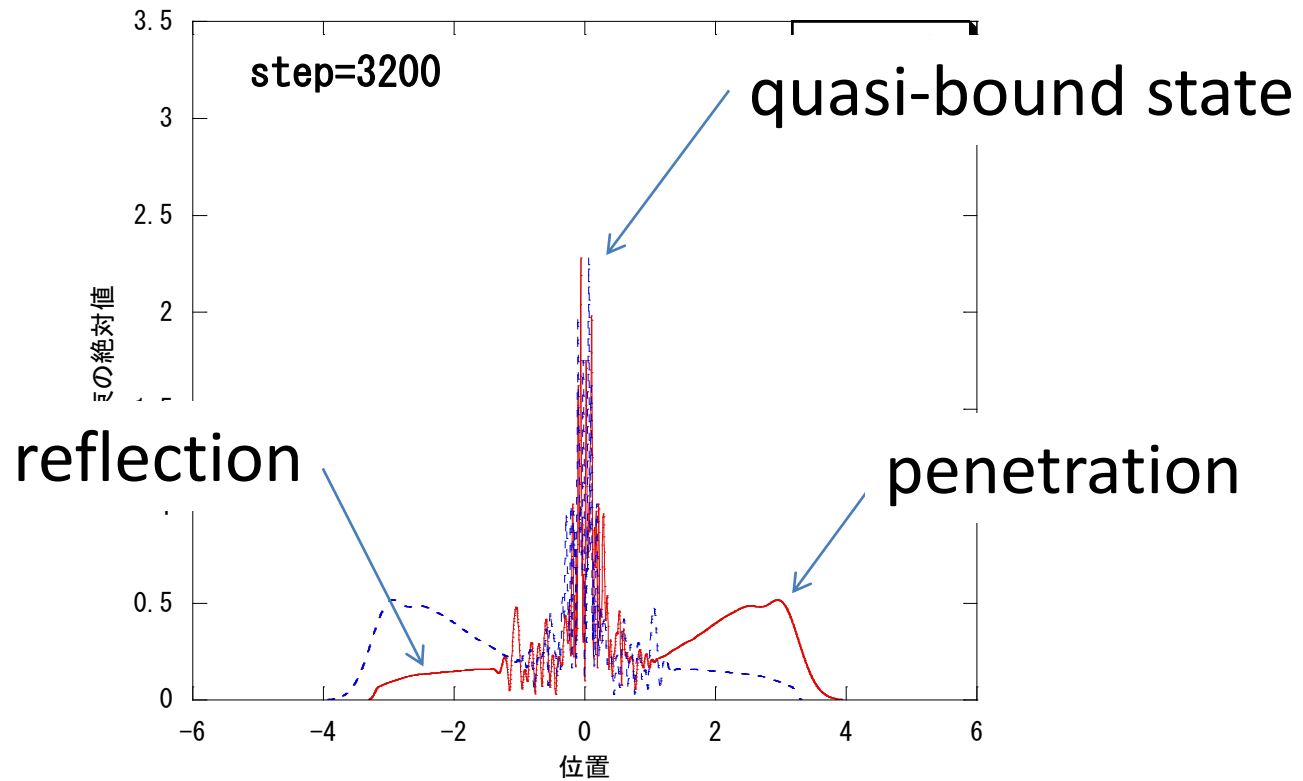
Wave?

$$i\hbar \frac{\partial}{\partial t} \psi(x, t) = \left( \hat{T} + V(x, t) \right) \psi(x, t)$$

$$\psi(x_i, x_j, t) = \phi_i(x_i, t) \phi_j(x_j, t)$$

# Time development of Gaussian wave packets





Cluster (correlation) = particle + wave

MC = Introduce probability to form a cluster

Probability should be determined to fit exp.

## 2<sup>nd</sup> question

Which processes should be included ?

Possible processes in forming a (deuteron) cluster

(1) indirect knockout  $p + \langle d \rangle$

(2) Higher order, rescattering  $\langle d \rangle + \langle N \rangle$

(3) Indirect pickup  $\Delta p \cdot \Delta x$

(4) Coalescence  $\Delta p \cdot \Delta x$  or  $\Delta E \cdot \Delta t$  ?

(5) direct (pickup, knockout) : shell state excitation

(6) direct formation  $p + \langle N \rangle = d + \pi$  or  $\gamma$



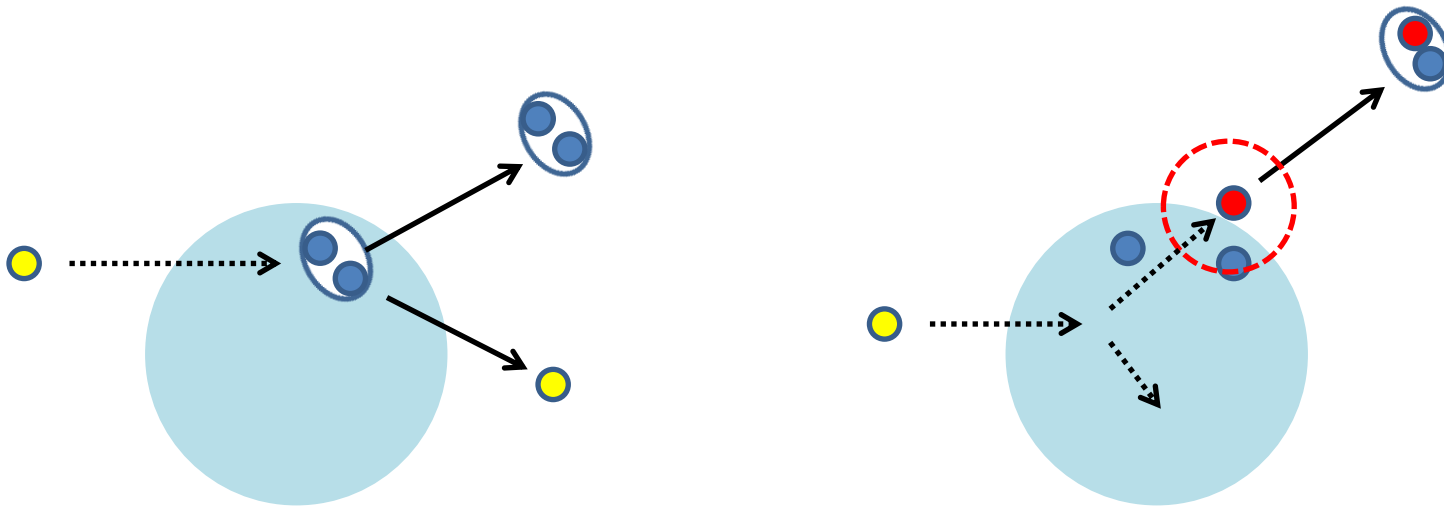
Previous studies on cluster productions

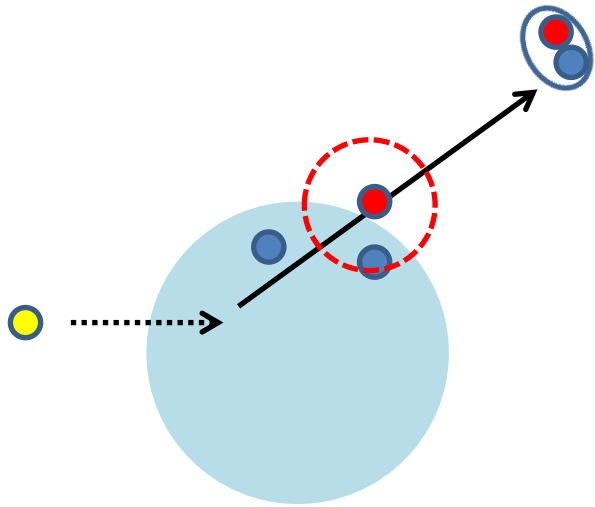
Many theoretical efforts

exciton model or hybrid model

two directions:

1. **knockout** (preformed cluster )
2. **coalescence** or **pickup**

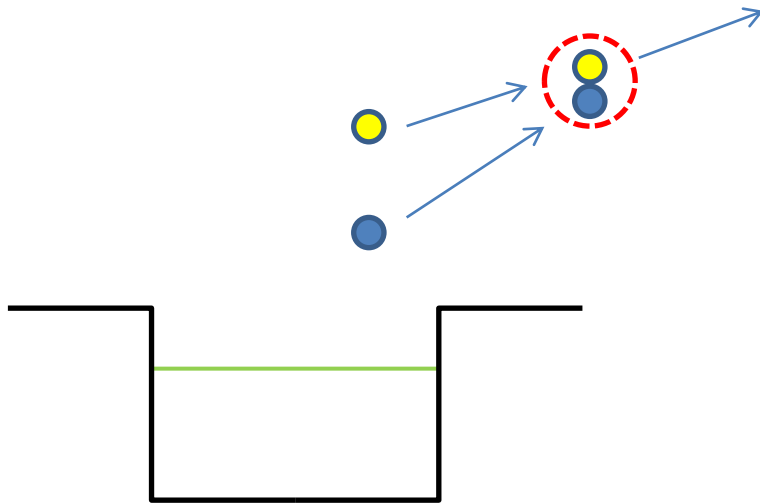




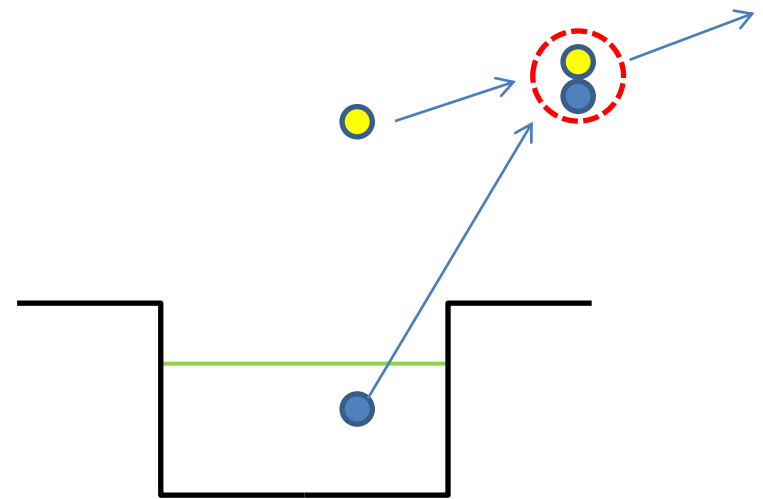
## coalescence / pickup

Lower energy, more chance to find a partner.  
Responsible for low energy cluster production

$$\Delta p \cdot \Delta x < C$$



coalescence



pickup

Why opposite pictures in exciton model studies?

Low beam energies below 100 MeV might cause this ambiguity.

higher beam energy 1 GeV?, less ambiguity.

**pickup** : lower energy part

Phase space limits high energy cluster

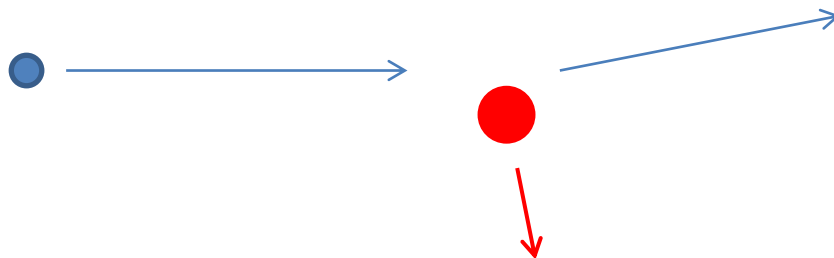
**knockout** : higher energy part of spectra  
preformed cluster  $\approx$  elementary particle

Both processes should be responsible.

Another ambiguity : knockout

The exciton model does not involve angular momentum.

forward-peaked angular distributions in  
experimental data  
impossible in classical cluster-knockout picture.  
N+<cluster> scattering  
cross section, Pauli blocking



(p,dx) reaction has been open question

- very weak binding of a deuteron
- probability to find a deuteron in a nucleus
- real d or virtual ? Pauli principle
- Nd scattering cross section, angular distribution, unknown
- disintegration probability after Nd scattering

(p,dx) spectrum

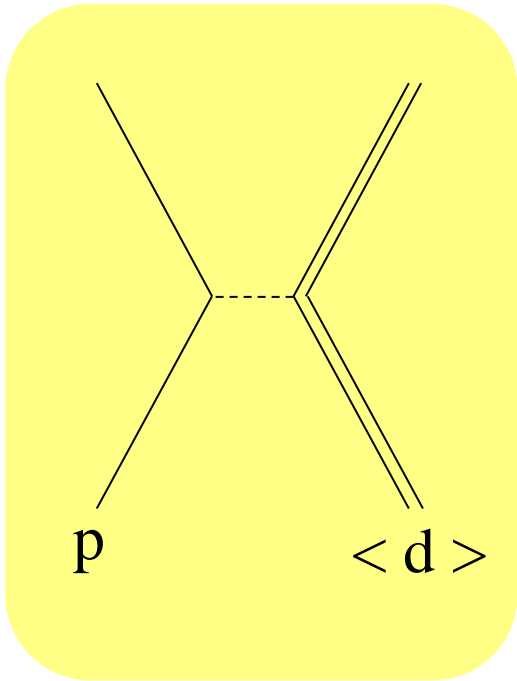
quasi-free like bump at forward angle.

real d + N scattering is not a forward peak distribution

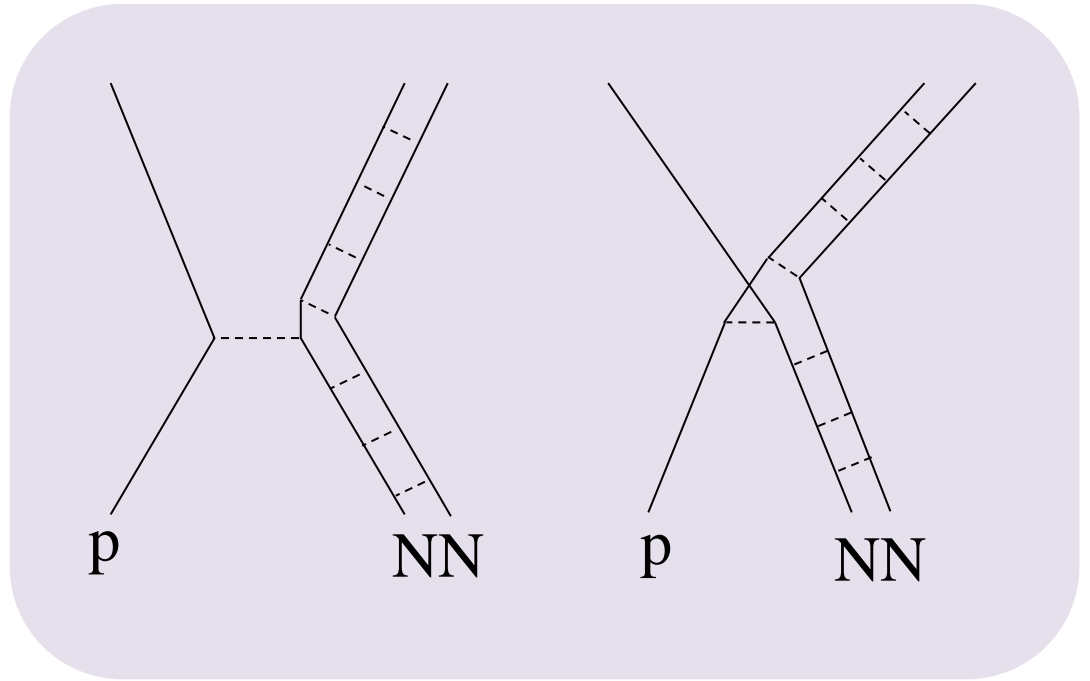
Strongly correlated pn pair

iso-spin forbidden transition in (e,e'd) reaction is explained in terms of the deuteron integration

# Cluster knockout



d =  
Elementary particle  
Non-perturbative



d = composite particle  
perturbative

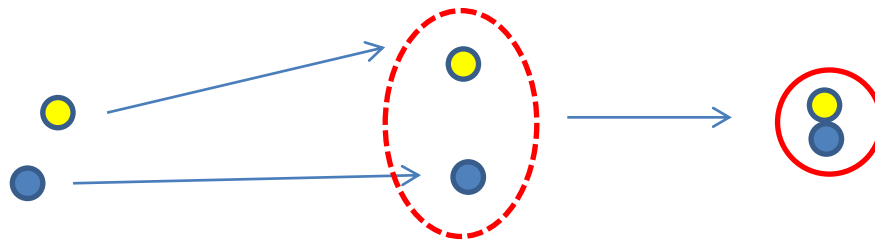
Forward peak ← exchange term  
NN cross section  
Pauli blocking

# QMD and AMD

= Molecular dynamics : attractive force

Coalescence like

relative momenta to CM should be small



Particle picture = phase space  $\Delta p \cdot \Delta x$

High-energy cluster formation = wave picture

Direct reaction = soft collision

wave function plays a role

Not classical picture

# Cluster formation requires binding at positive energy

## initial state

gr.st. cluster    the higher order in single particle states

(1) indirect knockout  $p + \langle d \rangle$

(2) Higher order, rescattering  $\langle d \rangle + \langle N \rangle$

$$\begin{aligned} |Gr\rangle = & c_1 |(s.p.)_A\rangle \\ & + c_2 |(s.p.)_{A-2}(d)_2\rangle \\ & + c_3 |(s.p.)_{A-4}(\alpha)_4\rangle \\ & + \dots \end{aligned}$$

## final state

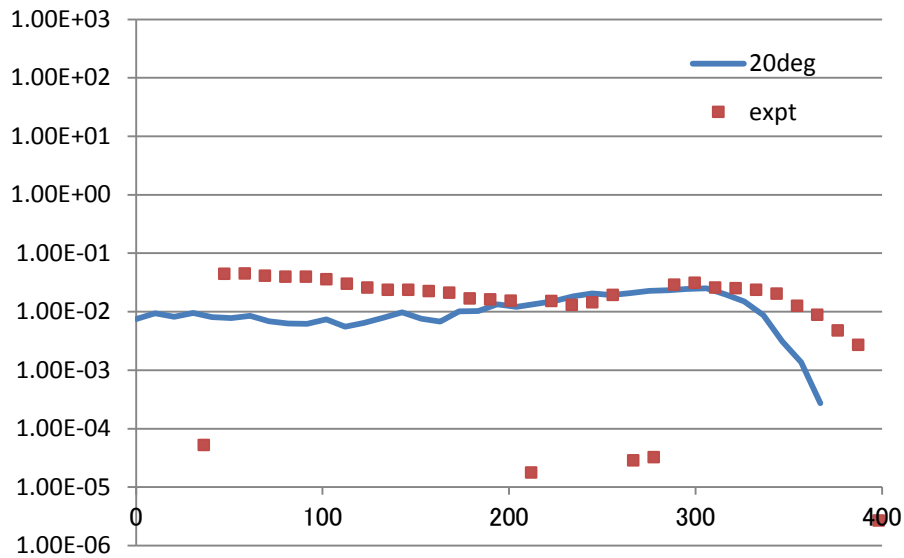
(3) Indirect pickup     $\Delta p \cdot \Delta x$

(4) Coalescence         $\Delta p \cdot \Delta x$

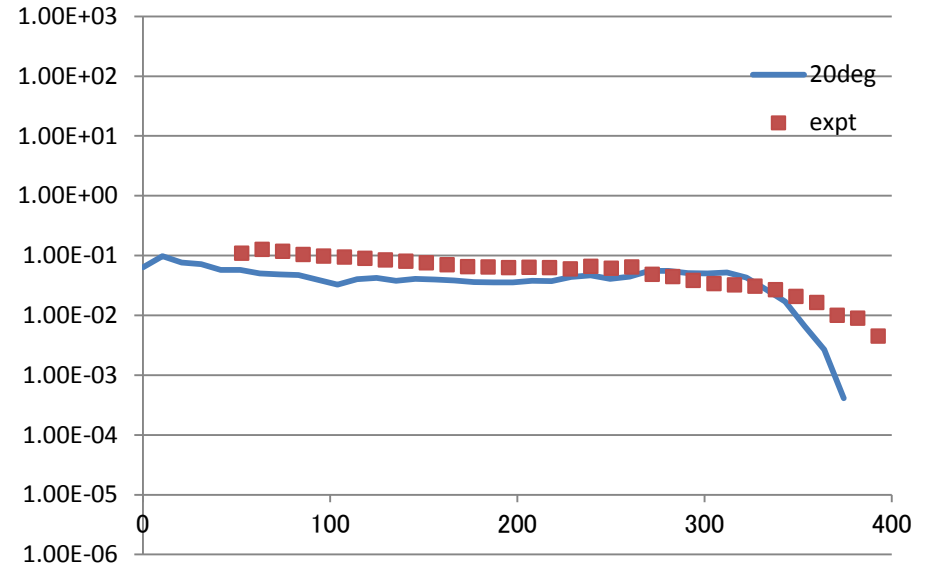


only knockout

**C(p,d) 392 MeV**



**V(p,d) 392 MeV**



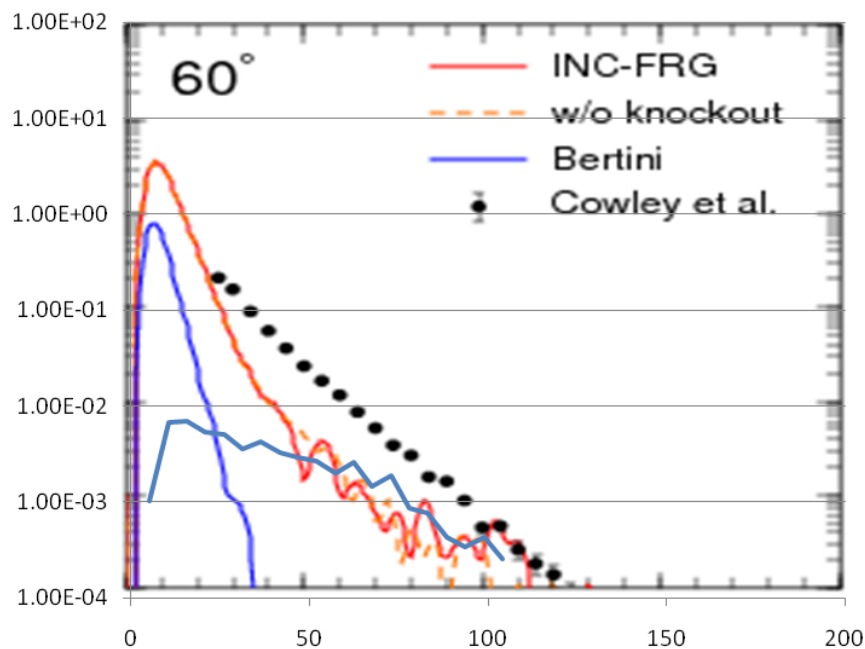
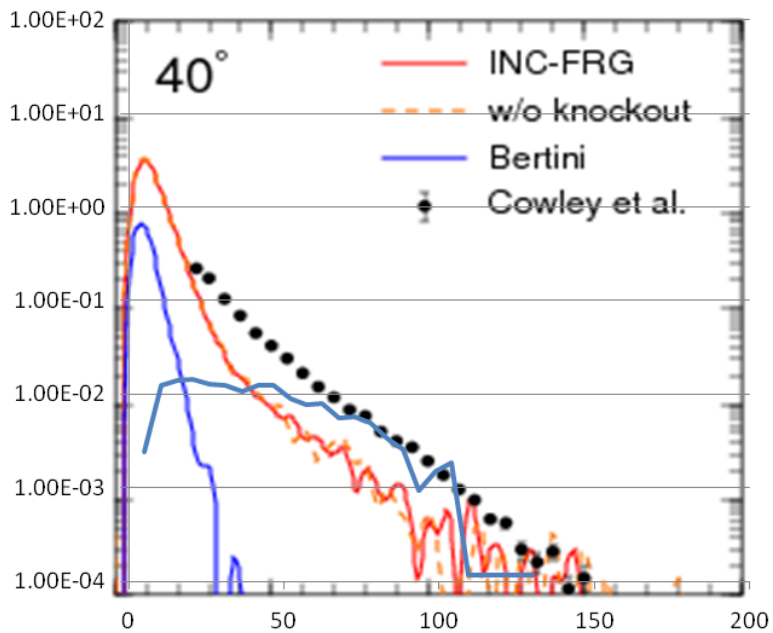
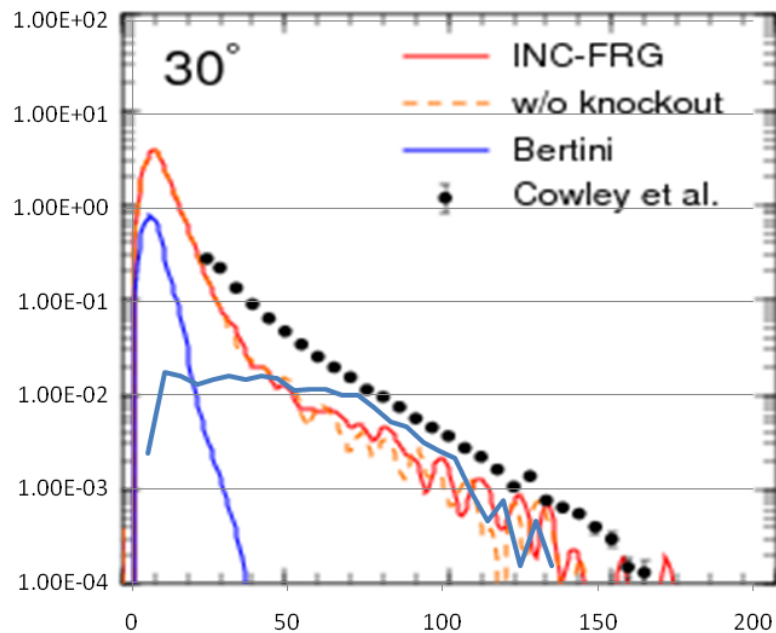
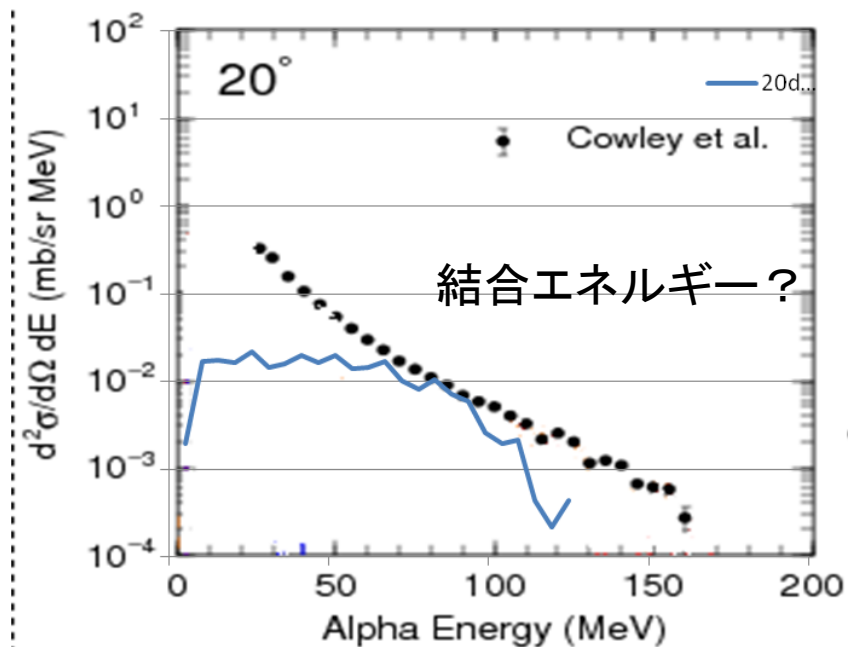
only knockout

Lower energy: indirect pickup, coalescence, evaporation

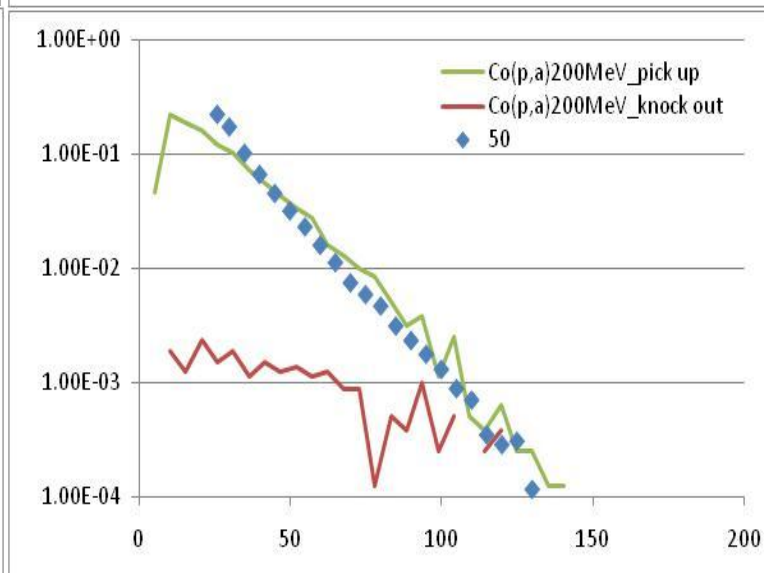
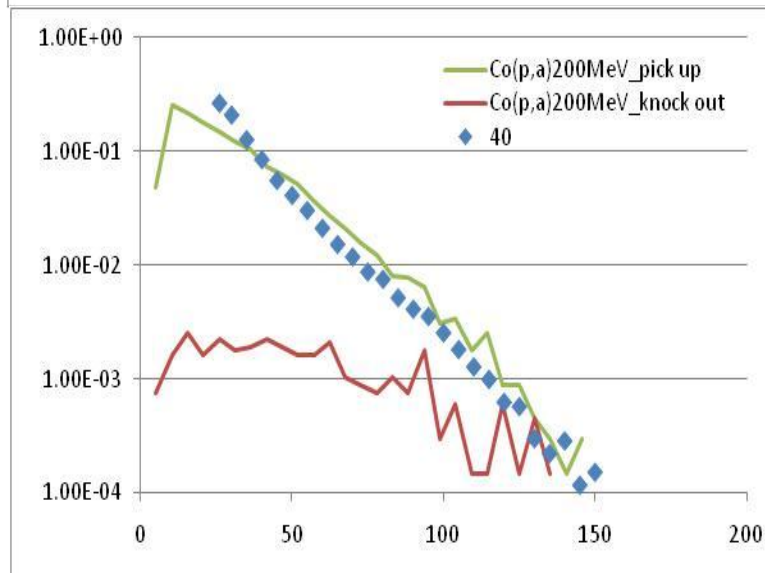
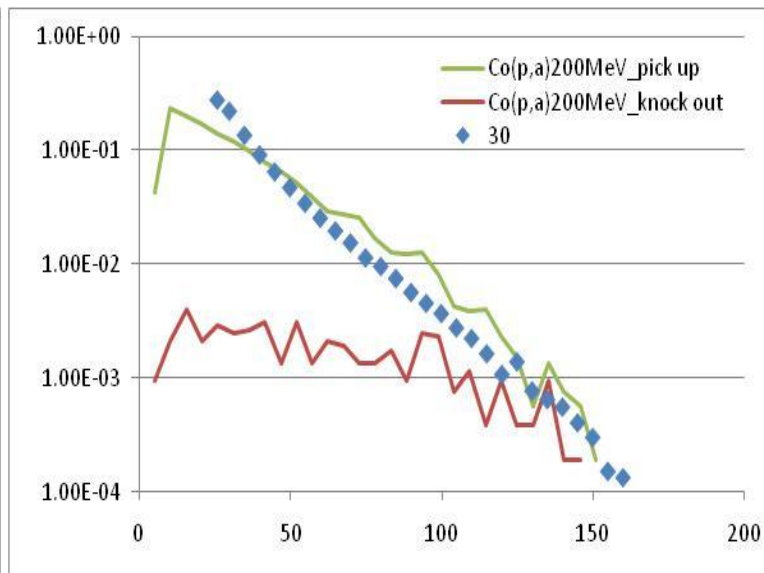
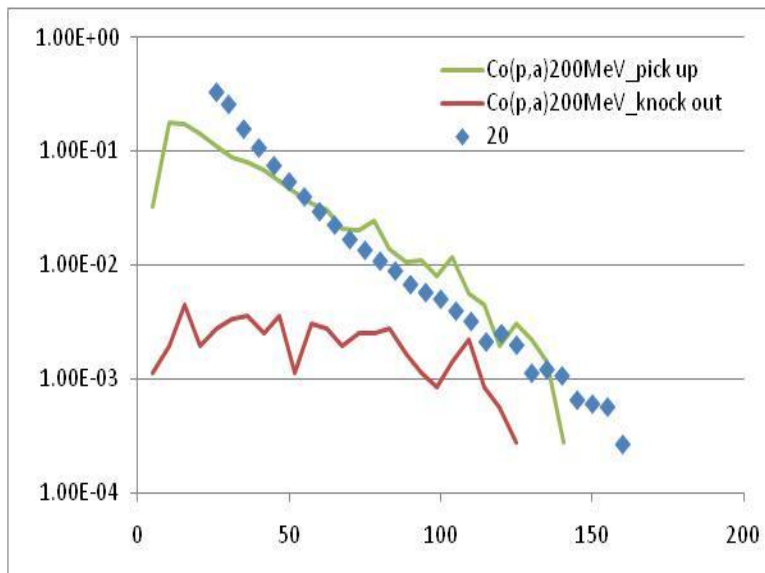
Highest energy :

- $p + \langle n \rangle = d$
- $p + \langle N \rangle = d + \pi$
- direct pickup

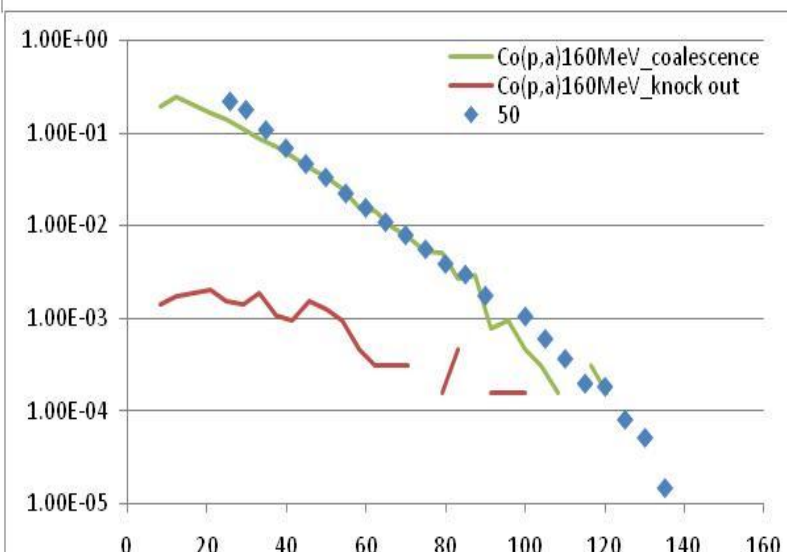
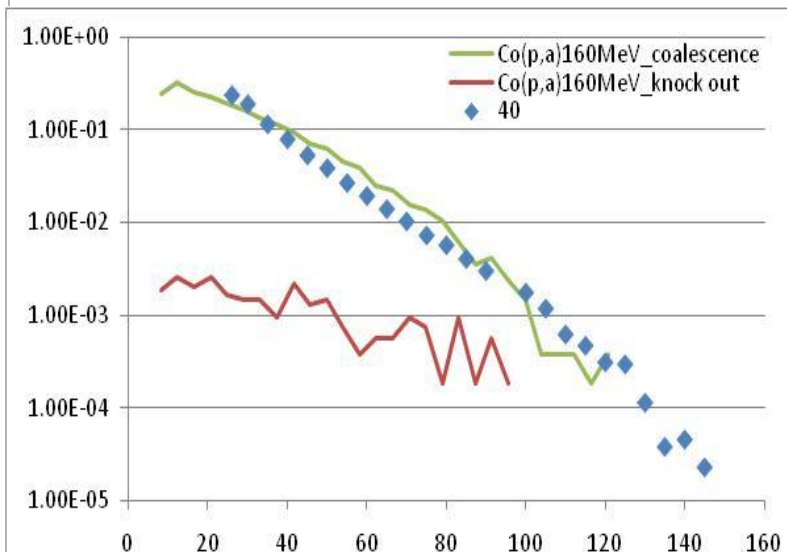
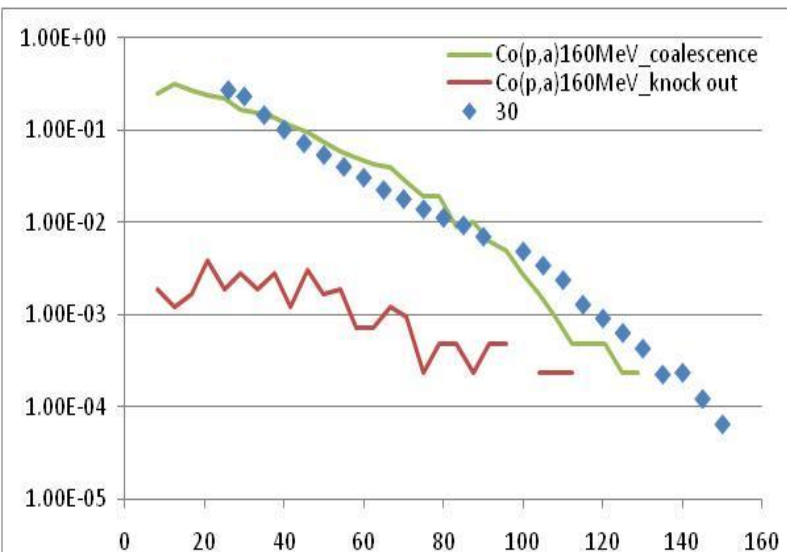
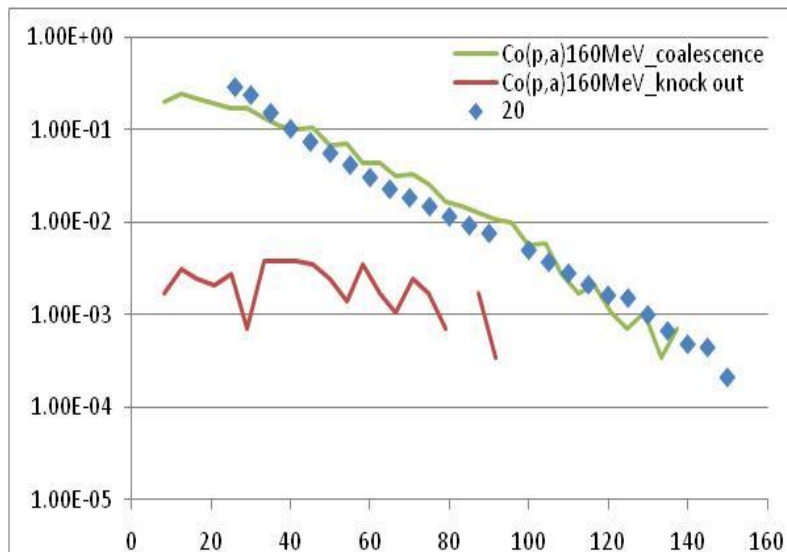
# Co(p, $\alpha$ ) at 200 MeV only knockout



# Co(p, $\alpha$ ) at 200 MeV pickup

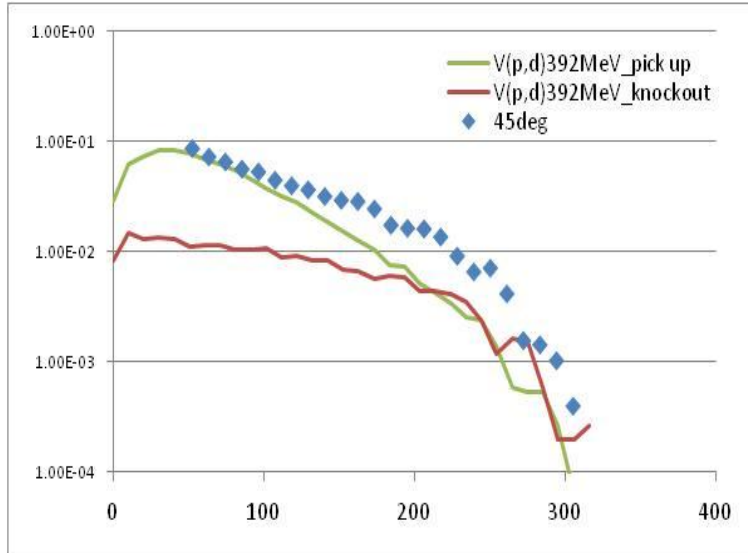


# Co(p, $\alpha$ ) at 160 MeV pickup

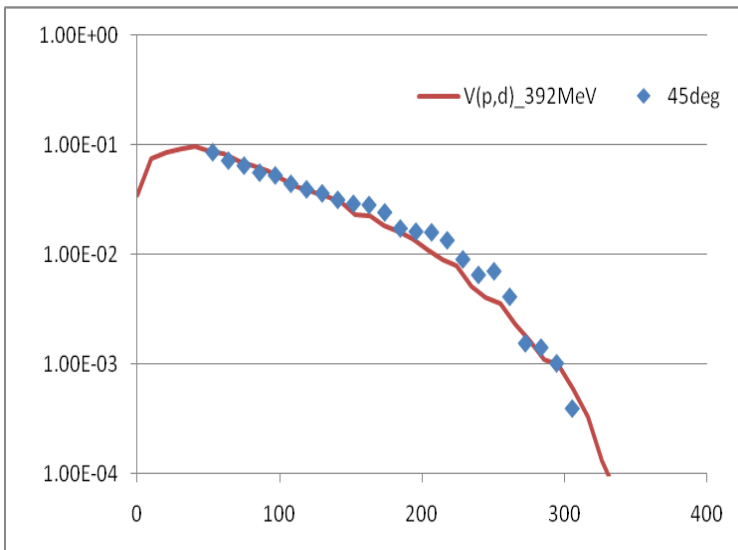


# V(p, d) at 392 MeV

pickup (green), and knockout (red)

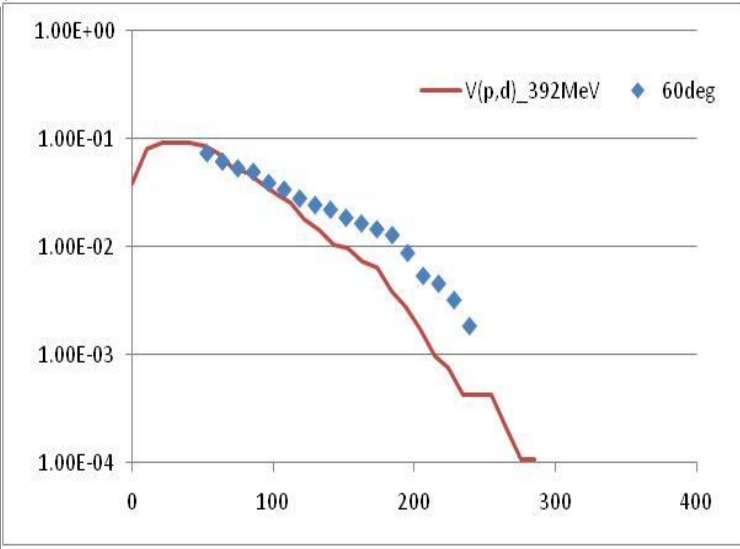
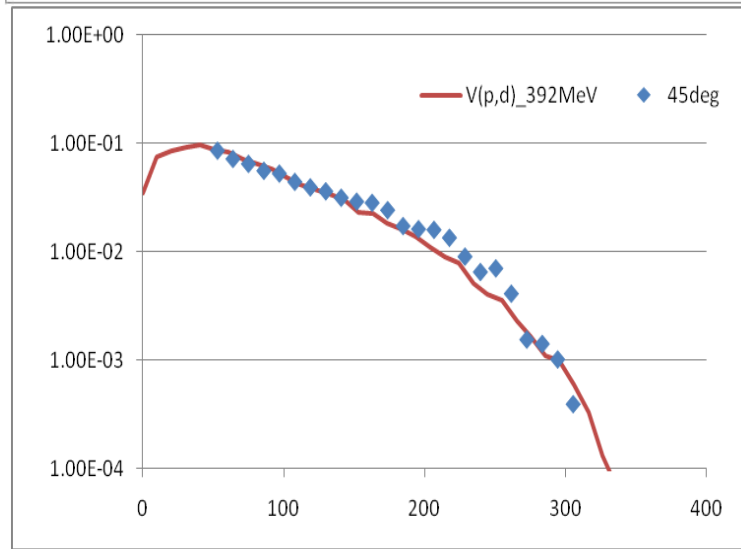
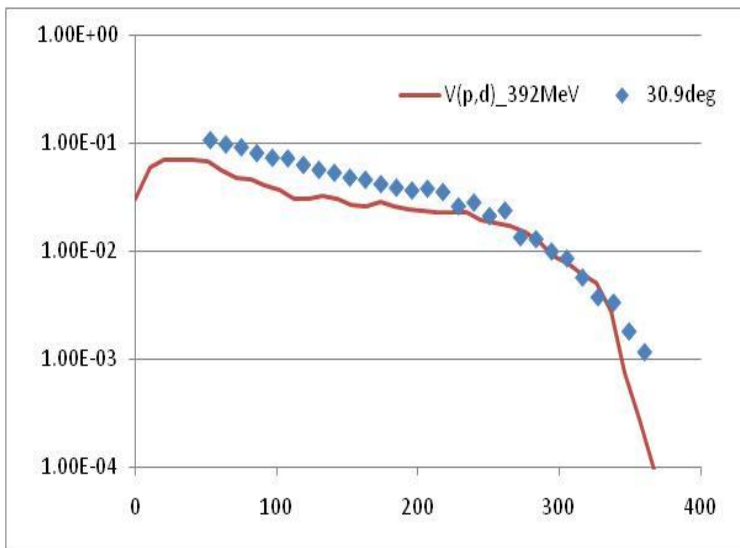
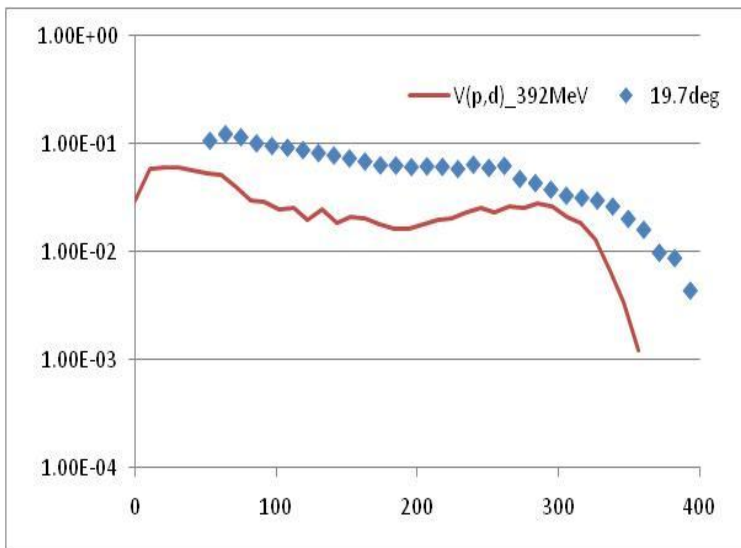


Pickup;  
Underestimate high-energy part

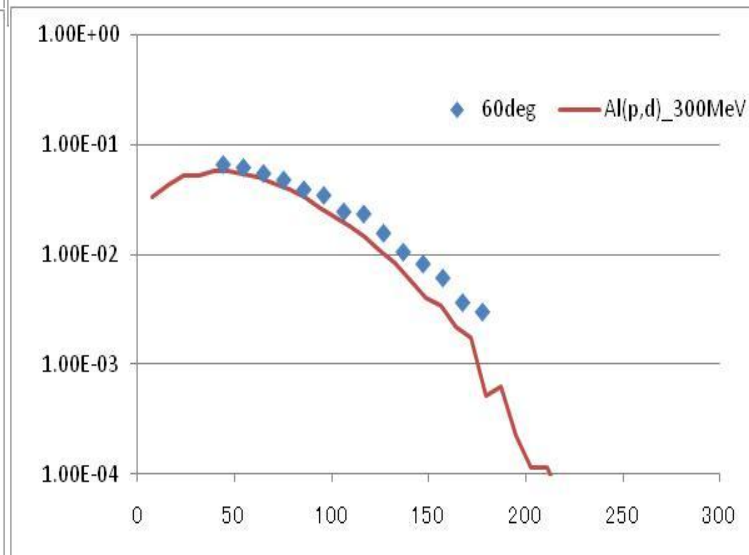
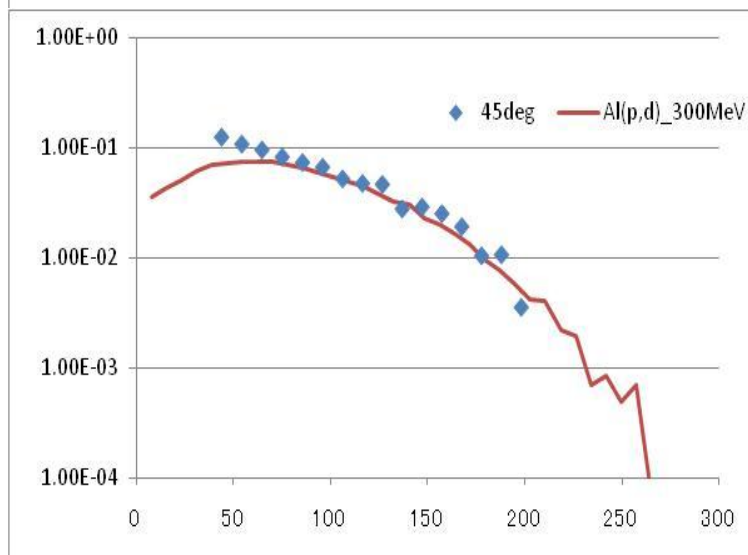
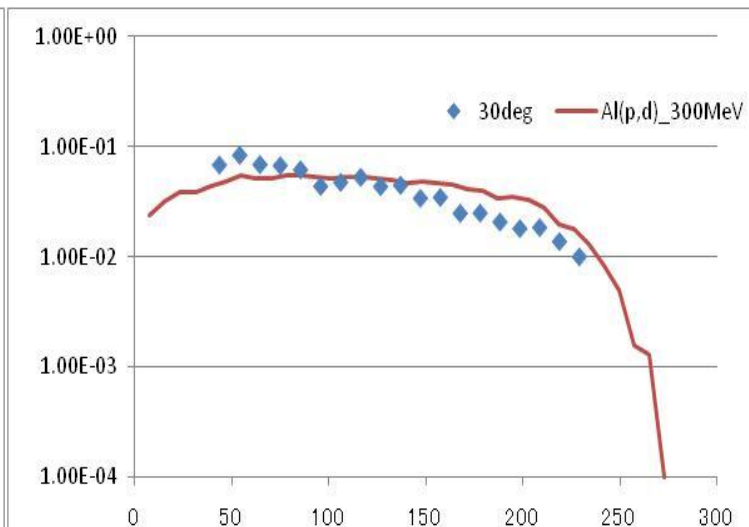
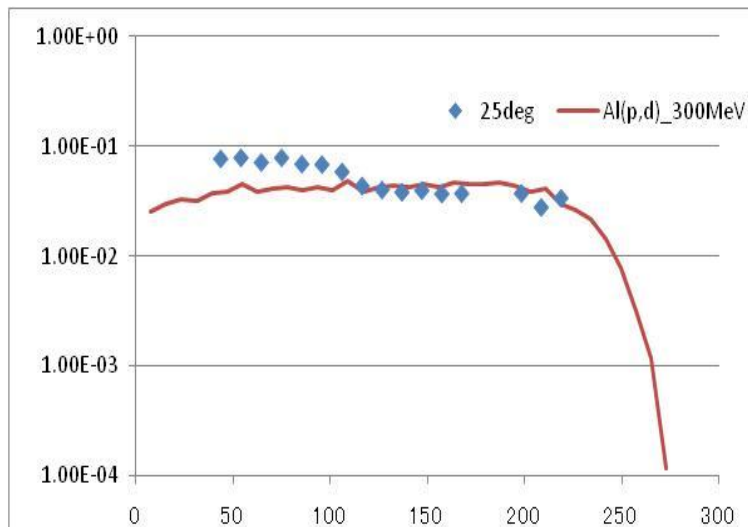


Sum of pickup and knockout

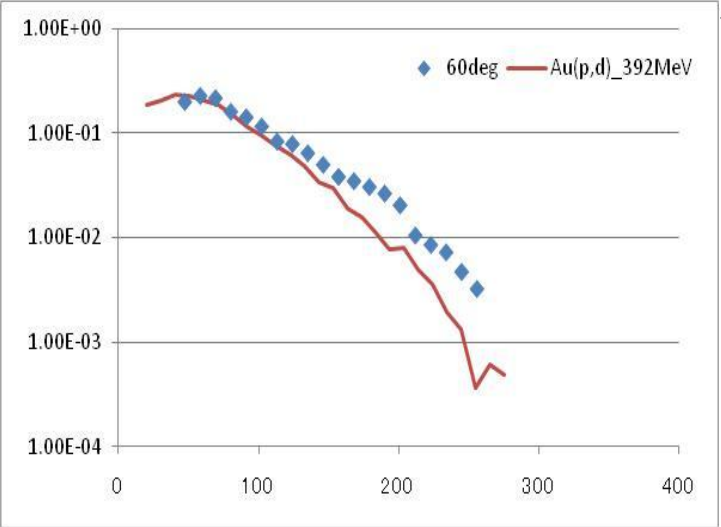
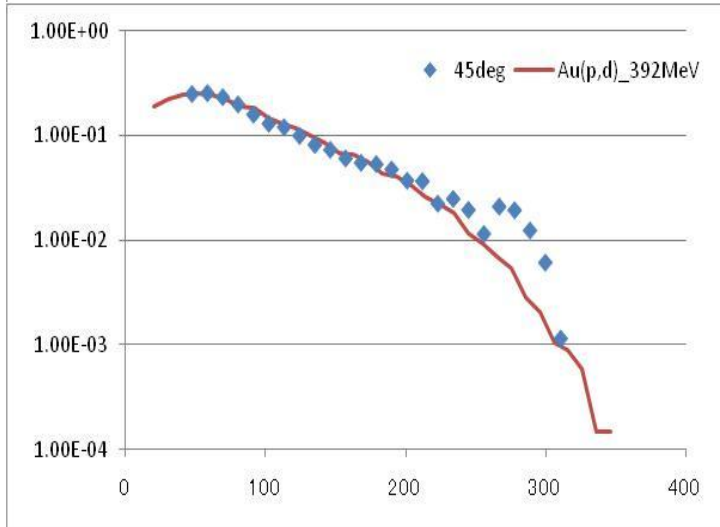
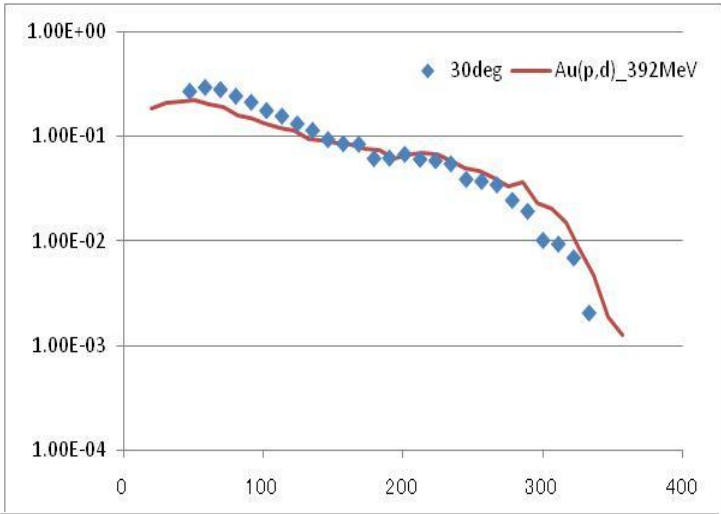
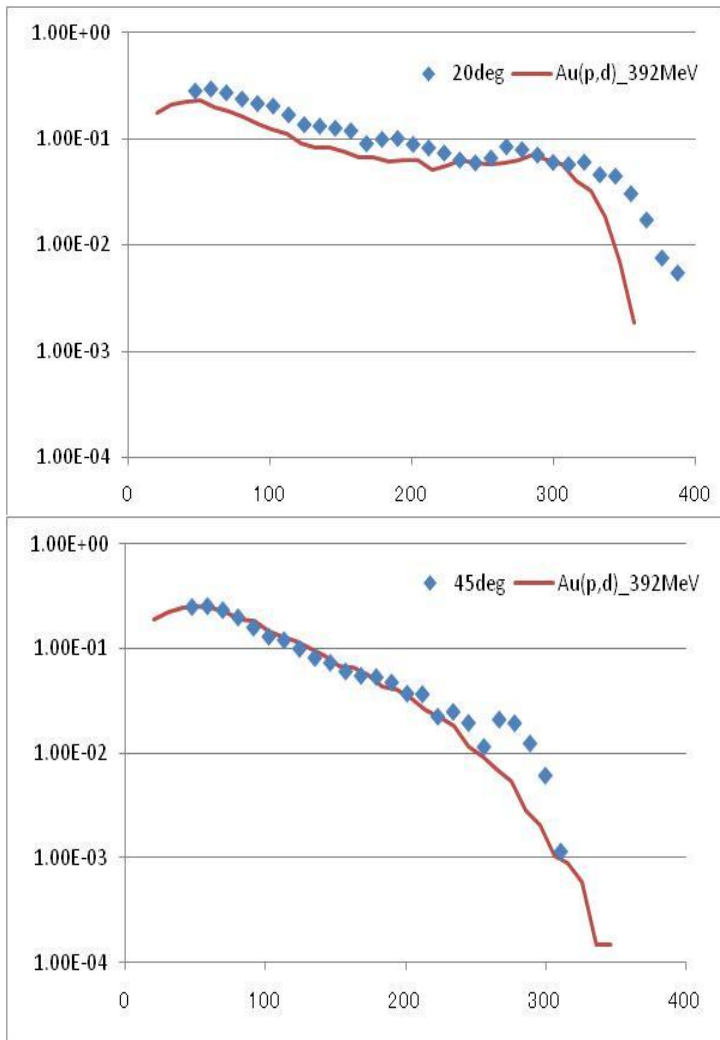
# V(p, d) at 392 MeV pickup + knockout



# Al(p, d) at 300 MeV pickup + knockout

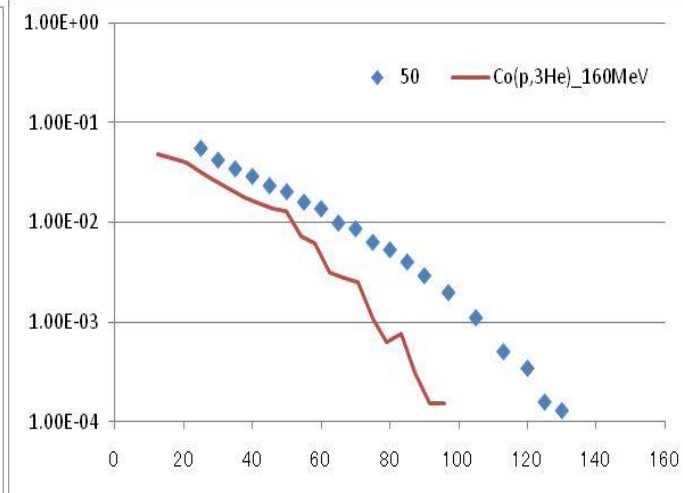
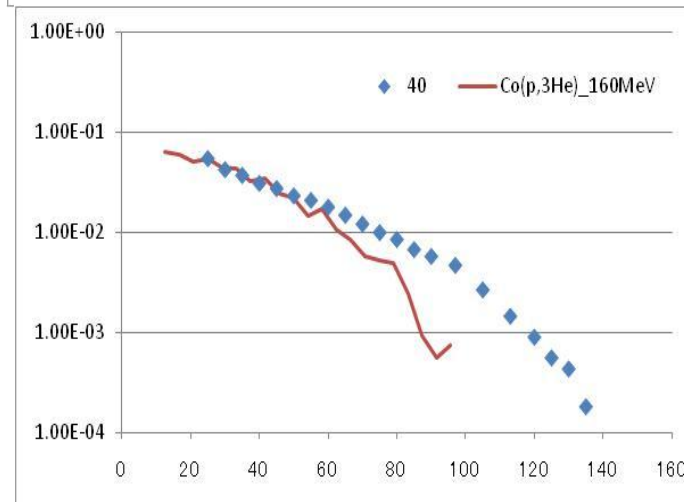
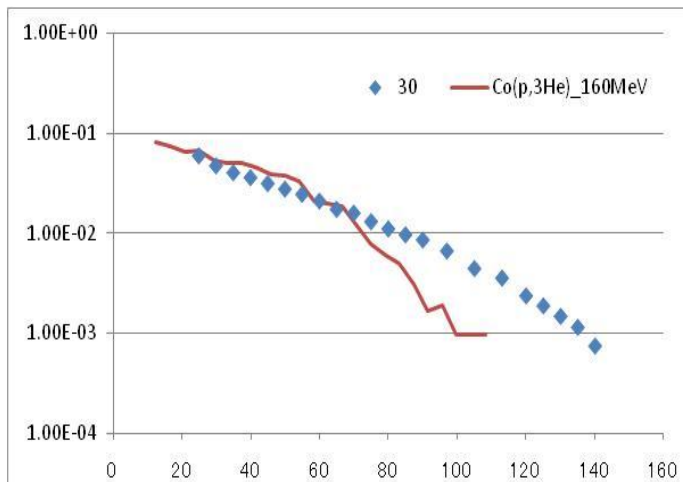
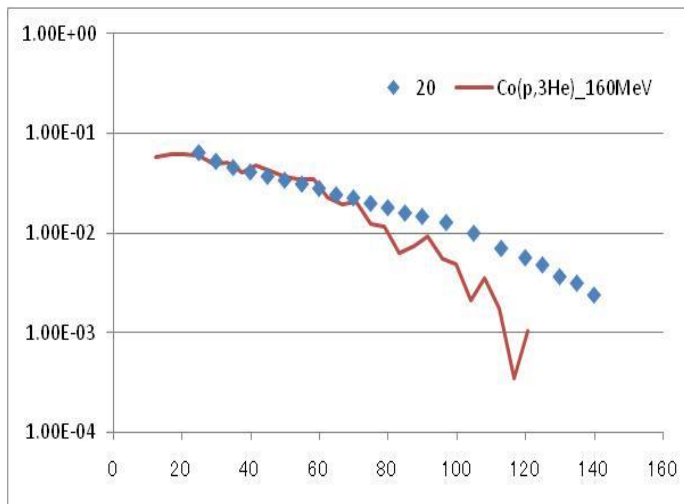


# Au(p, d) at 392 MeV pickup + knockout

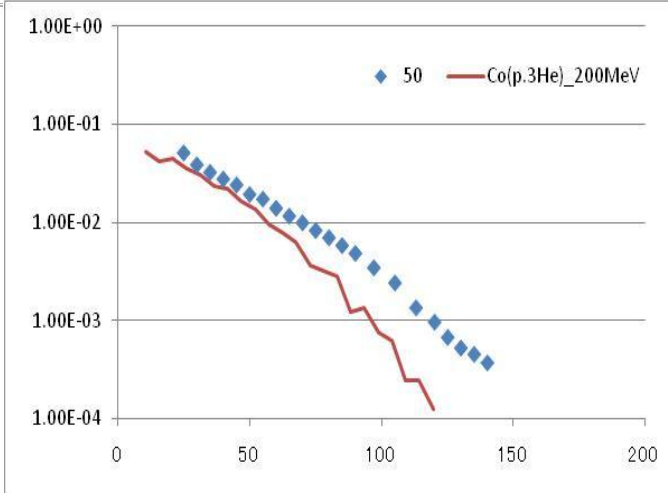
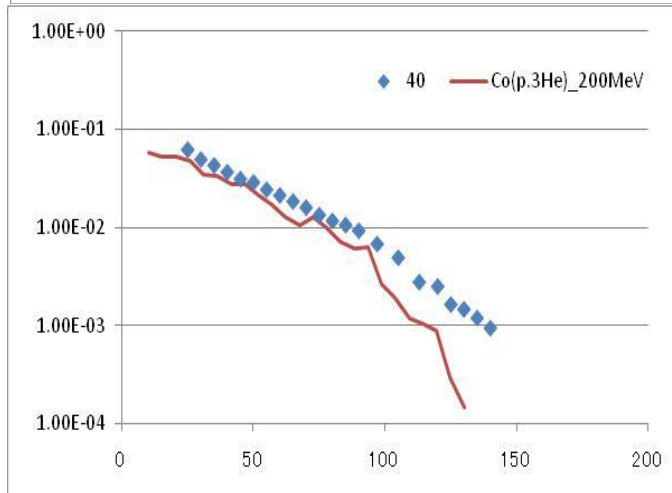
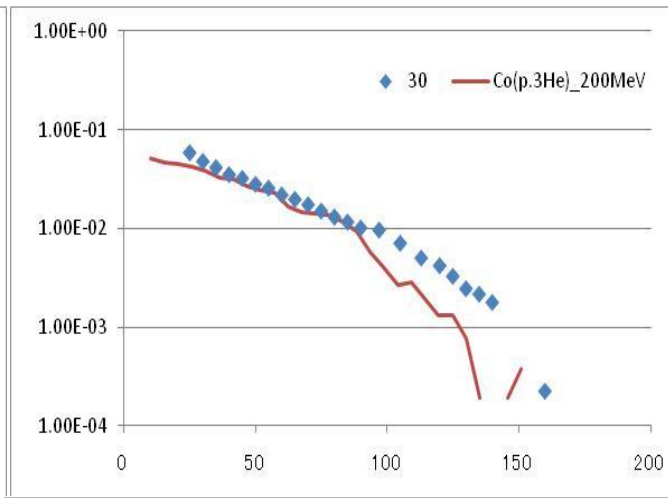
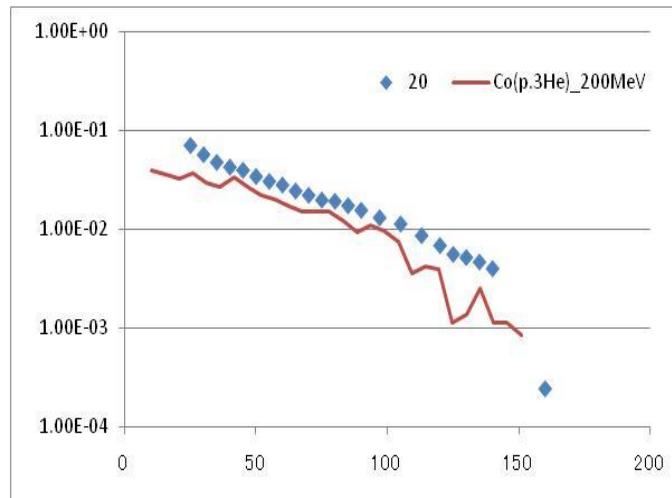




# Co(p, 3He) at 160 MeV pickup + knockout



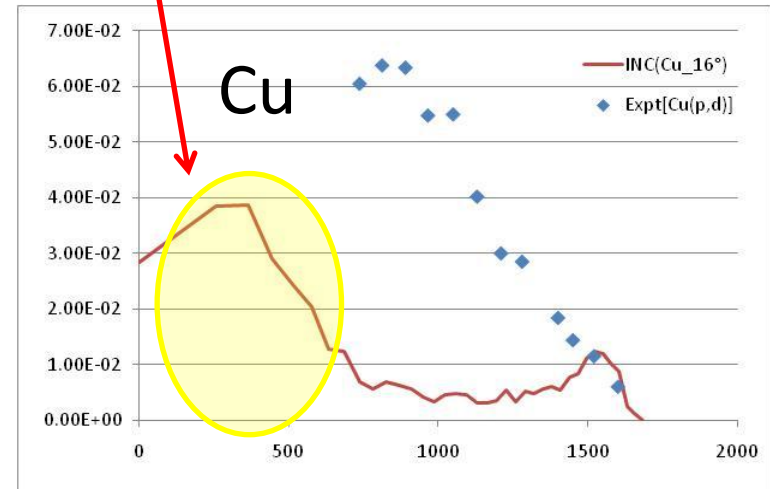
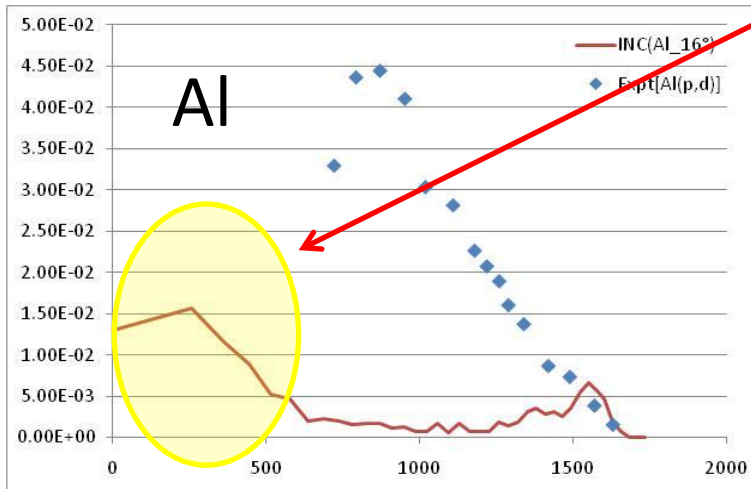
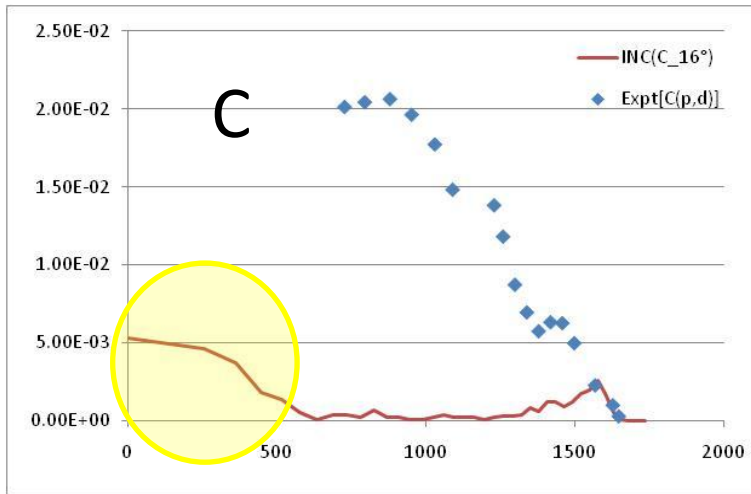
# Co(p, 3He) at 200 MeV pickup + knockout



(p,d) at 670 MeV, 16deg

Only elastic NN scattering

Inelastic influences KO  
need more KO



pickup ; No high-energy

# Summary

INC light cluster production (p,d), (p,3He), (p,  $\alpha$ )  
pickup and knockout

## Case 1; **More pickup**

Overall good accounts

for (p,d), (p,3He), (p,  $\alpha$ )

underestimation: 392-MeV (p,d) 20deg

670-MeV (p,d) 16 deg

## Case 2; **only knockout**

Overall good accounts for (p,d), (p,  $\alpha$ )

670-MeV (p,d) 16 deg ???

$\leq 400$  MeV good

$\geq 600$  MeV  $\Delta$ ,  $\pi$ , knockout/pickup